

# Using Stochastic Programming to Improve Service Quality in an Outpatient Infusion Center

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# Current Team

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# Cancer and Cancer Treatment

- Cancer Statistics
  - 1,638,910 new cases of cancer in the United States (2012)
  - Second leading cause of death in the United States
- Outpatient Oncology
  - 29.2 million visits in the US with a primary diagnosis of cancer
  - 23 million adult patient visits for chemotherapy
  - 84% of visits for chemotherapy occur in the outpatient setting
- Chemotherapy Infusion Center
  - Facility where cancer treatment is given on an outpatient basis



# University of Michigan Comprehensive Cancer Center

- 1 of 41 United States centers to earn the National Cancer Institute “Comprehensive” designation
- 93,319 Outpatient Visits
- 51,884 Infusion Treatments



# Infusion Center Challenges

- Long patient waiting times
- Heavy nurse workload
  - Overtime
  - Equity
  - Safety concerns
- High demand for outpatient oncology services
- Cost
  - Nurse utilization
  - Pharmaceutical waste

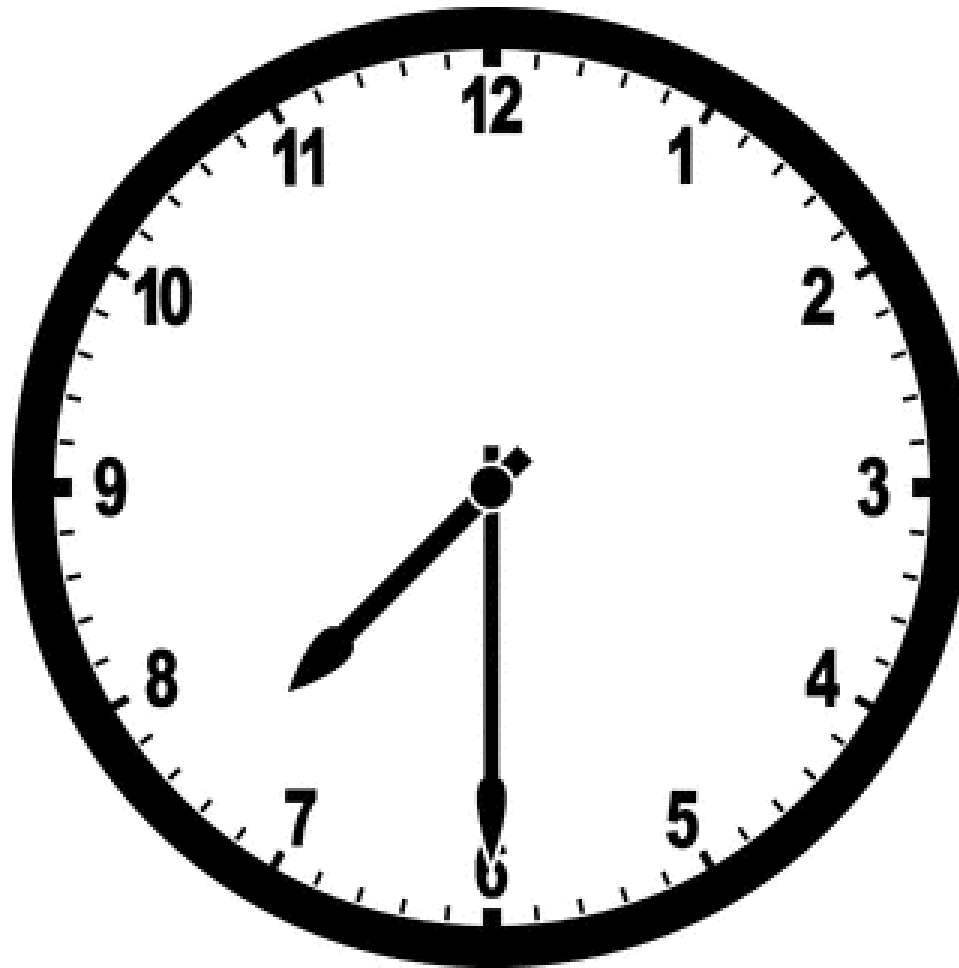


# Meet Mrs. J

- 52 y.o. woman diagnosed with Small Cell Carcinoma of the Cervix
- Chemotherapy regimen: Day 1: Cisplatin + Etoposide; Day 2 & 3: Hydration
- Scheduled infusion time: Day 1: 300 minutes; Day 2 & 3: 150 minutes
- Protocol: 4-6 Cycles, Every third week
- Travel: 60 miles each way



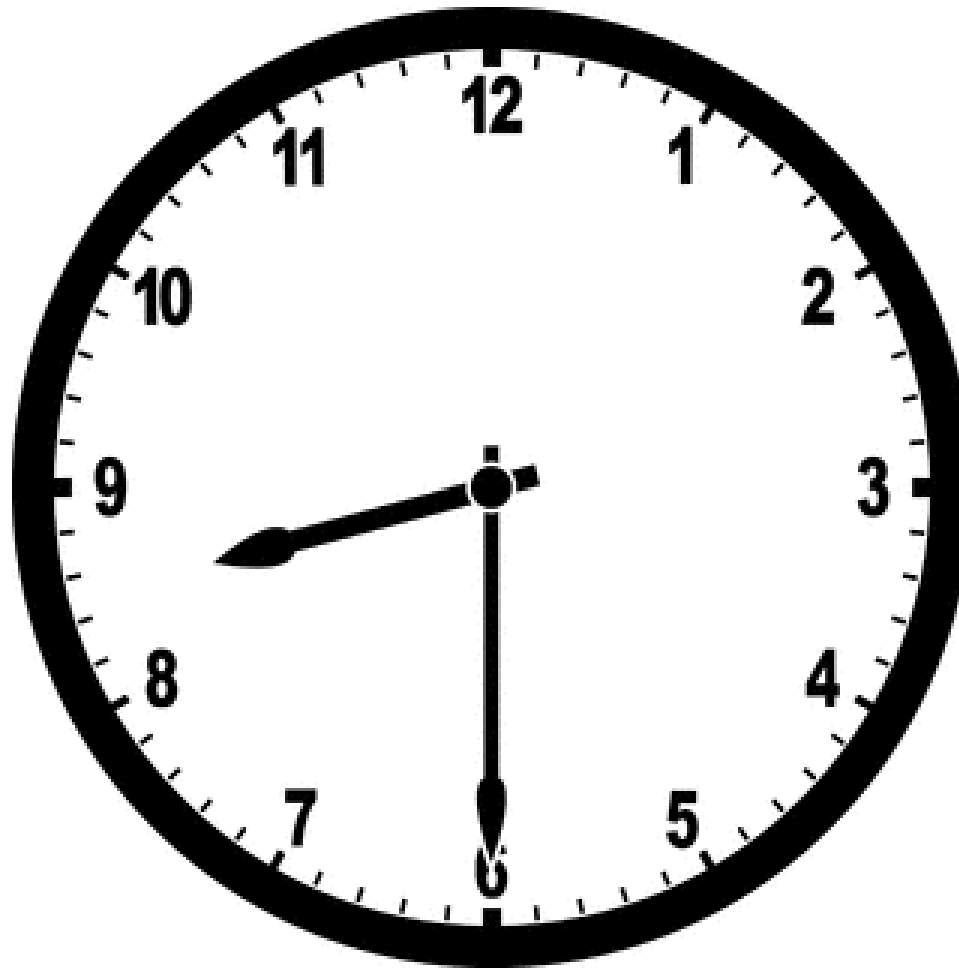
# Appointment 1: Lab Draw



7:30 am – Lab Draw



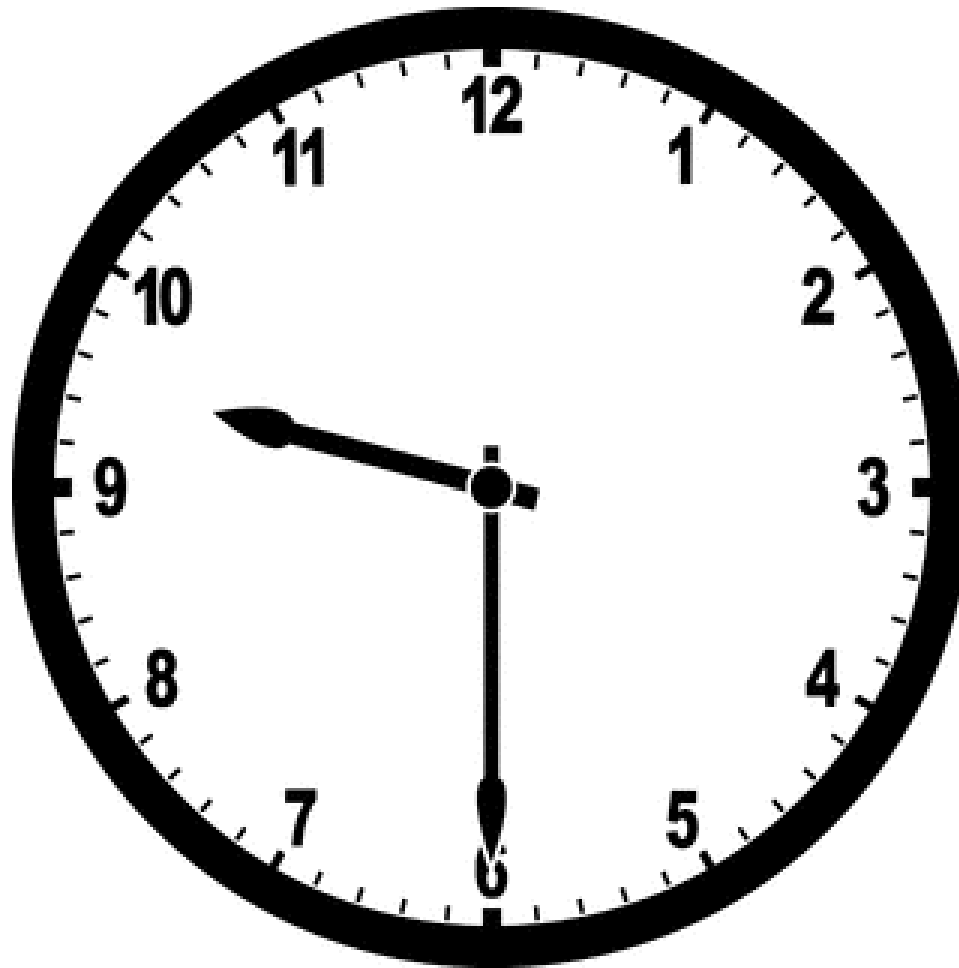
# Appointment 2: Clinic



7:30 am – Lab Draw

8:30 am – Clinic

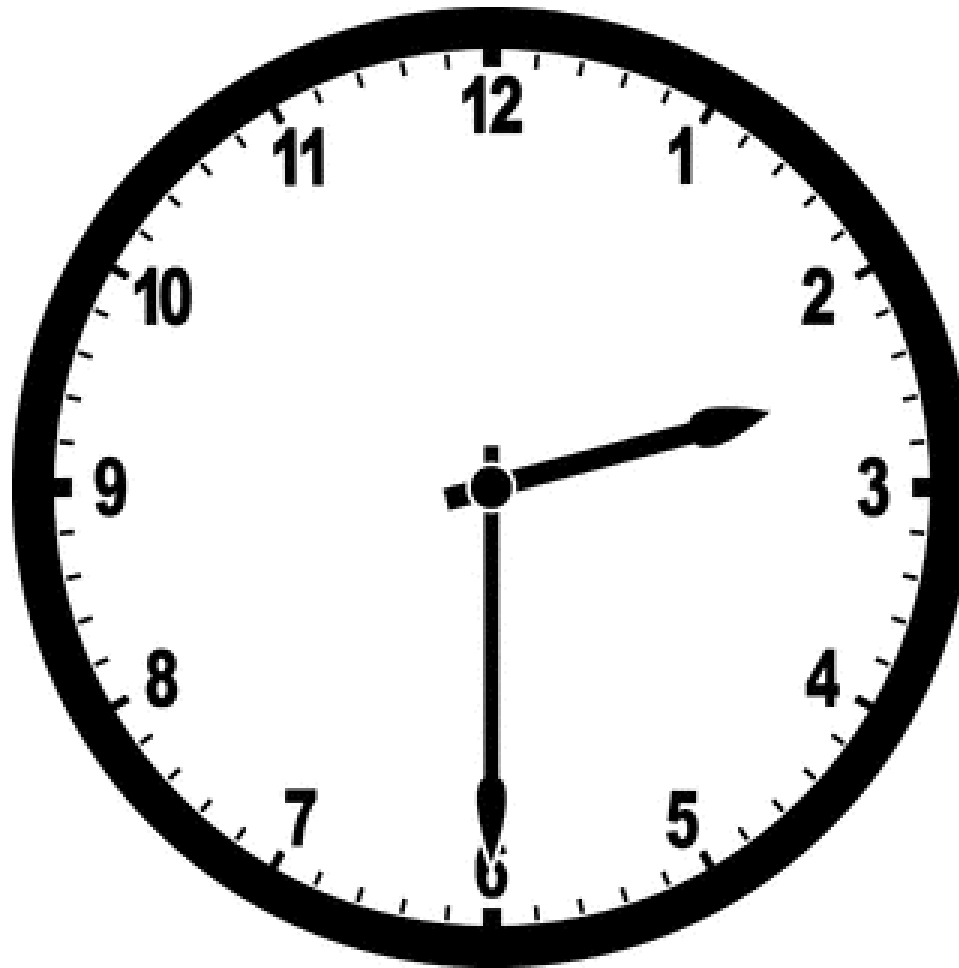
# Appointment 3: Infusion



7:30 am – Lab Draw  
8:30 am – Clinic  
9:30 am – Infusion



# Mrs. J Leaves



7:30 am – Lab Draw  
8:30 am – Clinic  
9:30 am – Infusion  
2:30 pm – Discharge



# During her visit to the Cancer Center...

- Mrs. J will spend 90 minutes waiting on average
- She will see 2 different nurses during her infusion
- She will not arrive home until 5:00 pm
- She will return to the Cancer Center at 07:30 am the next two days for two hours of hydration each day.

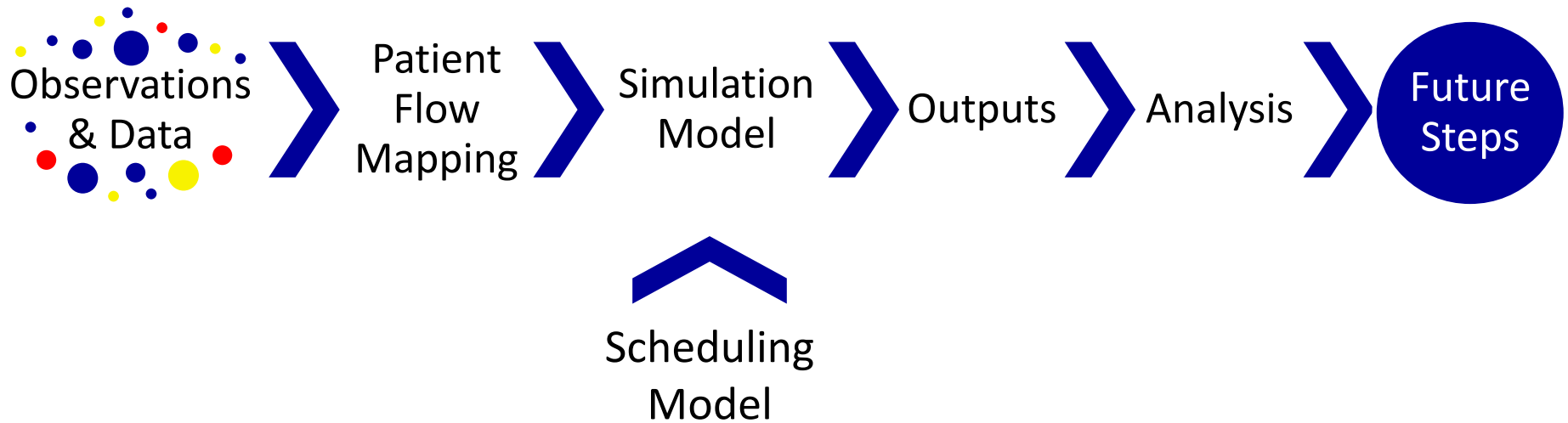


# Project Goals

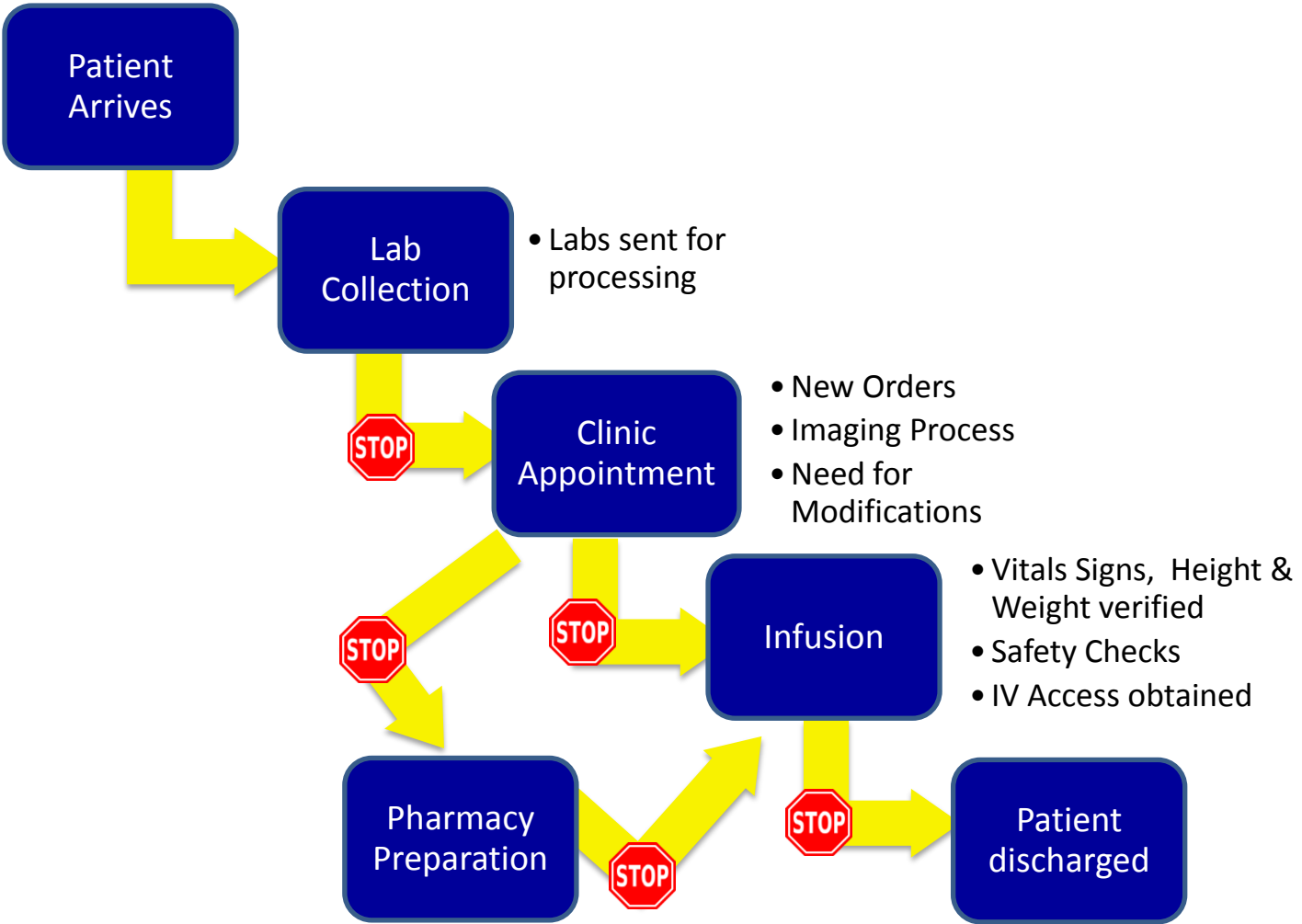
- Improve quality of cancer care delivery in the infusion center
  - Reduce patient waiting times
  - Reduce total length of day of operations
  - Improve patient and nurse safety



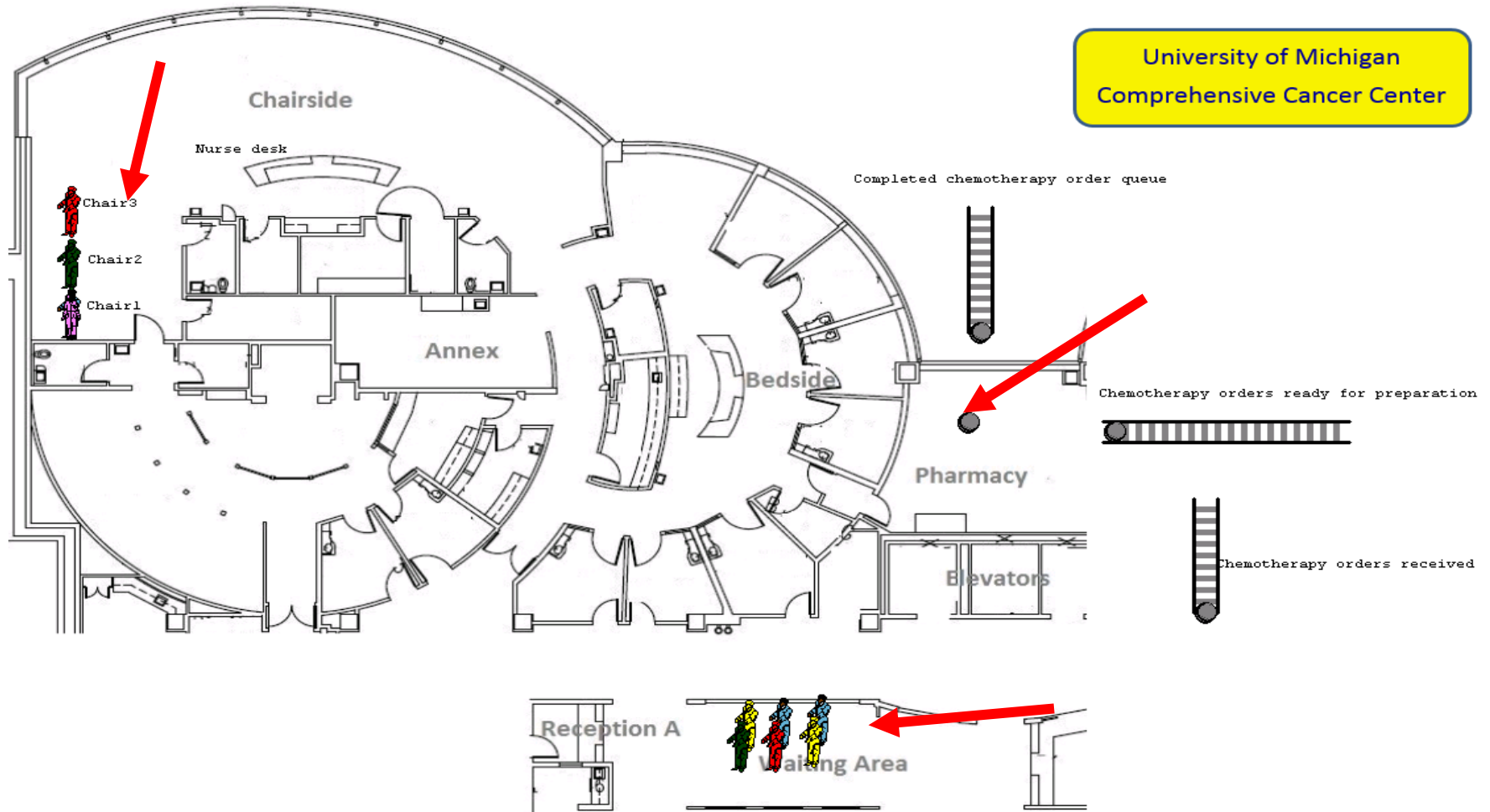
# Approach



# Patient Flow



# Computer Simulation Model





# Computer Simulation Model

## Inputs - Outputs

### Inputs

Patient types

Nurse preparation time

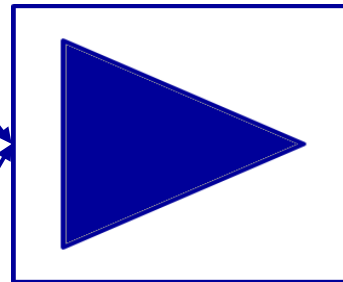
Nurse discharge time

Pharmacy preparation time

Patient appointment schedules

- Baseline
- LPT heuristic
- SPT heuristic
- Stochastic model

### Computer Simulation



### Outputs

Average patient waiting times

Hours of operation

Chair utilization

Average time in system



# LPT and SPT Sequencing Rules

- Patient arrivals are sequenced based on the mean of their infusion time distribution
  - LPT: Longest treatment time first
  - SPT: Shortest treatment time first



# Stochastic Scheduling Model

- Generates appointment schedule that reduces patient waiting times and total length of operations for a workday
- Nature
  - Large scale MIP model
- Stochasticity
  - Scenarios represent variability
  - Scenarios sample infusion, preparation and discharge times from distributions
- Results
  - Appointment times
  - Patient sequence
  - Patient-Chair assignment



# Stochastic Scheduling Model Formulation

## Decision Variables

$a_p$  : appointment time of patient  $p$

$w_p^\omega$  : waiting time of patient  $p$  in scenario  $\omega$

$d_p^\omega$  : exit time of patient  $p$  in scenario  $\omega$

$x_{pc}^\omega$  : binary, 1 if patient  $p$  is assigned to chair  $c$  in scenario  $\omega$ ; 0 otherwise

$z_{p'p}$  : binary, 1 if patient  $p'$  is scheduled before patient  $p$ ; 0 otherwise

$L^\omega$  : end of day in scenario  $\omega$

## Parameters

$s_p^\omega$  : preparation time of patient  $p$  in scenario  $\omega$

$t_p^\omega$  : infusion time plus discharge time of patient  $p$  in scenario  $\omega$

$m$  : number of scenarios

$\lambda$  : weight in the objective function

$M$  : large number



# Stochastic Scheduling Model Formulation

$$\min_{a,z,x^\omega,d^\omega,w^\omega,E^\omega} \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega$$

Objective Function: Trade-off between the total expected waiting time and the expected end of day



# Stochastic Scheduling Model Formulation

$$\begin{aligned} \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} \quad & \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\ \text{subject to} \quad & \sum_{c \in C} x_{pc}^\omega = 1 \qquad \forall p \in P, \forall \omega \in \Omega \end{aligned}$$

Each patient should be assigned to exactly one infusion chair



# Stochastic Scheduling Model Formulation

$$\begin{aligned} \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} \quad & \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\ \text{subject to} \quad & \sum_{c \in C} x_{pc}^\omega = 1 && \forall p \in P, \forall \omega \in \Omega \\ & a_p + w_p^\omega + s_p^\omega + t_p^\omega = d_p^\omega && \forall p \in P, \forall \omega \in \Omega \end{aligned}$$

Value of exit time of patient p in each scenario



# Stochastic Scheduling Model Formulation

$$\begin{aligned}
 & \min_{a,z,x^\omega,d^\omega,w^\omega,E^\omega} \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\
 & \text{subject to} \quad \sum_{c \in C} x_{pc}^\omega = 1 \quad \forall p \in P, \forall \omega \in \Omega \\
 & \quad a_p + w_p^\omega + s_p^\omega + t_p^\omega = d_p^\omega \quad \forall p \in P, \forall \omega \in \Omega \\
 & \quad a_p + w_p^\omega + M(3 - x_{pc}^\omega - x_{p'c}^\omega - z_{p'p}) \geq d_{p'}^\omega \quad \forall c \in C, \forall p, p' \in P, \forall \omega \in \Omega
 \end{aligned}$$

Free chair constraint: A patient can sit in a chair only if all previously sequenced patients assigned to the same chair have been discharged





# Stochastic Scheduling Model Formulation

$$\begin{aligned}
 & \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} && \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\
 & \text{subject to} && \sum_{c \in C} x_{pc}^\omega = 1 && \forall p \in P, \forall \omega \in \Omega \\
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 & && a_p + w_p^\omega + M z_{pp'} \geq a_{p'} + w_{p'}^\omega + s_{p'}^\omega && \forall p, p' \in P, \forall \omega \in \Omega
 \end{aligned}$$

Available nurse constraint: A patient can sit in a chair if the nurse has finished preparing all previously sequenced patients



# Stochastic Scheduling Model Formulation

$$\begin{aligned}
 & \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} && \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\
 & \text{subject to} && \sum_{c \in C} x_{pc}^\omega = 1 && \forall p \in P, \forall \omega \in \Omega \\
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 & && a_p + w_p^\omega + M z_{pp'} \geq a_{p'} + w_{p'}^\omega + s_{p'}^\omega && \forall p, p' \in P, \forall \omega \in \Omega \\
 & && L^\omega \geq d_p^\omega && \forall p \in P, \forall \omega \in \Omega
 \end{aligned}$$

All patients should be discharged to end the day



# Stochastic Scheduling Model Formulation

$$\begin{aligned}
 & \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} && \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\
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 & && a_p + w_p^\omega + M z_{pp'} \geq a_{p'} + w_{p'}^\omega + s_{p'}^\omega && \forall p, p' \in P, \forall \omega \in \Omega \\
 & && L^\omega \geq d_p^\omega && \forall p \in P, \forall \omega \in \Omega \\
 & && (a_{p'} - a_p) + M(z_{p'p}) \geq 0 && \forall p, p' \in P \\
 & && z_{pp'} = 1 - z_{p'p} && \forall p, p' \in P
 \end{aligned}$$

Definition of variable  $z_{p'p}$



# Stochastic Scheduling Model Formulation

$$\begin{aligned}
 & \min_{a, z, x^\omega, d^\omega, w^\omega, E^\omega} \lambda \sum_{p \in P} \sum_{\omega \in \Omega} \frac{1}{m} w_p^\omega + (1 - \lambda) \sum_{\omega \in \Omega} \frac{1}{m} L^\omega \\
 & \text{subject to} \quad \sum_{c \in C} x_{pc}^\omega = 1 && \forall p \in P, \forall \omega \in \Omega \\
 & a_p + w_p^\omega + s_p^\omega + t_p^\omega = d_p^\omega && \forall p \in P, \forall \omega \in \Omega \\
 & a_p + w_p^\omega + M(3 - x_{pc}^\omega - x_{p'c}^\omega - z_{p'p}) \geq d_{p'}^\omega && \forall c \in C, \forall p, p' \in P, \forall \omega \in \Omega \\
 & a_p + w_p^\omega + M z_{pp'} \geq a_{p'} + w_{p'}^\omega + s_{p'}^\omega && \forall p, p' \in P, \forall \omega \in \Omega \\
 & L^\omega \geq d_p^\omega && \forall p \in P, \forall \omega \in \Omega \\
 & (a_{p'} - a_p) + M(z_{p'p}) \geq 0 && \forall p, p' \in P \\
 & z_{pp'} = 1 - z_{p'p} && \forall p, p' \in P \\
 & x_{pc}^\omega \in \{0, 1\} && \forall c \in C, \forall p \in P, \forall \omega \in \Omega \\
 & z_{p'p} \in \{0, 1\} && \forall p, p' \in P \\
 & a_p \geq 0 && \forall p \in P \\
 & w_p^\omega, d_p^\omega \geq 0 && \forall p \in P, \forall \omega \in \Omega
 \end{aligned}$$

Binary and non-negativity constraints

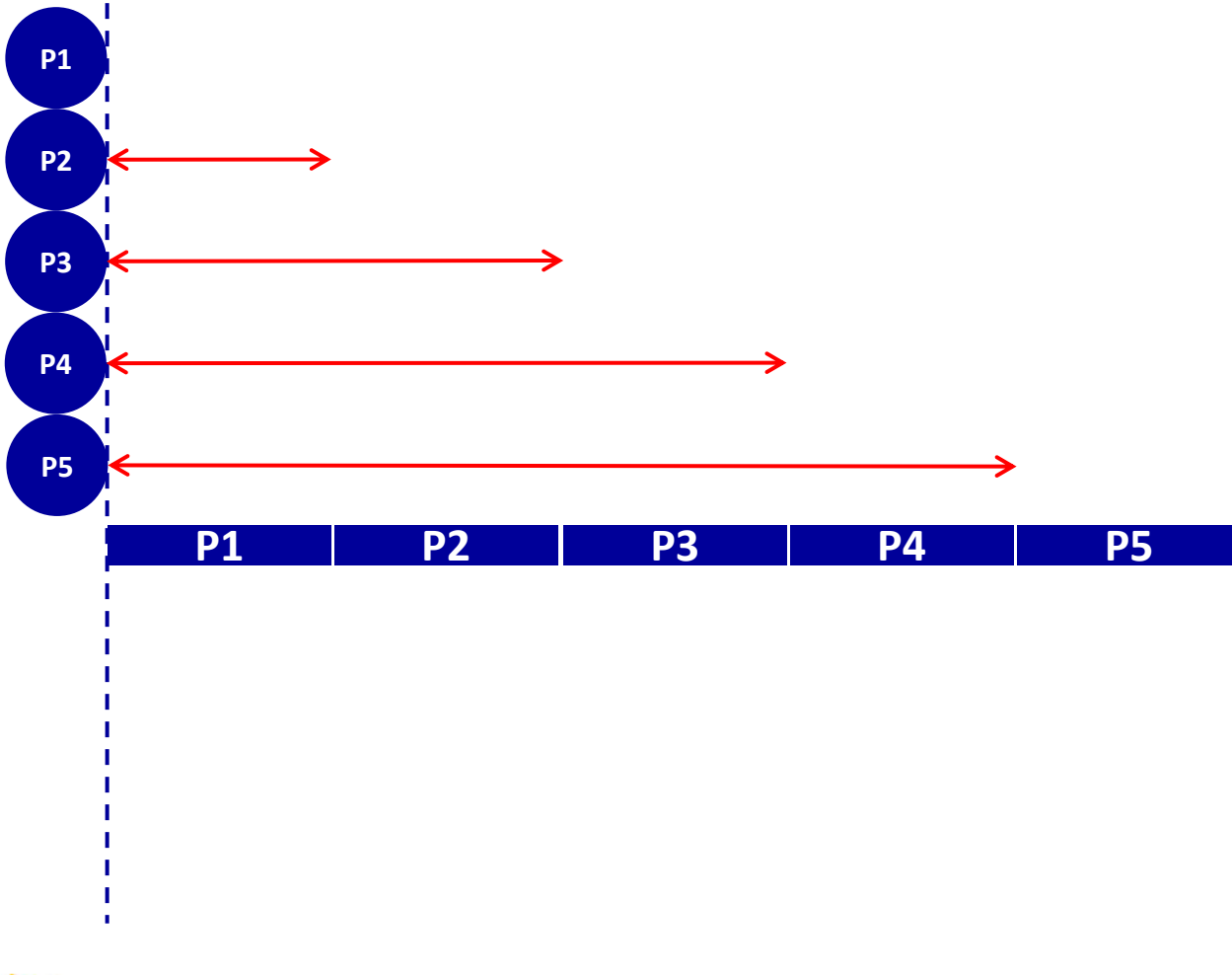


# Model Simplification

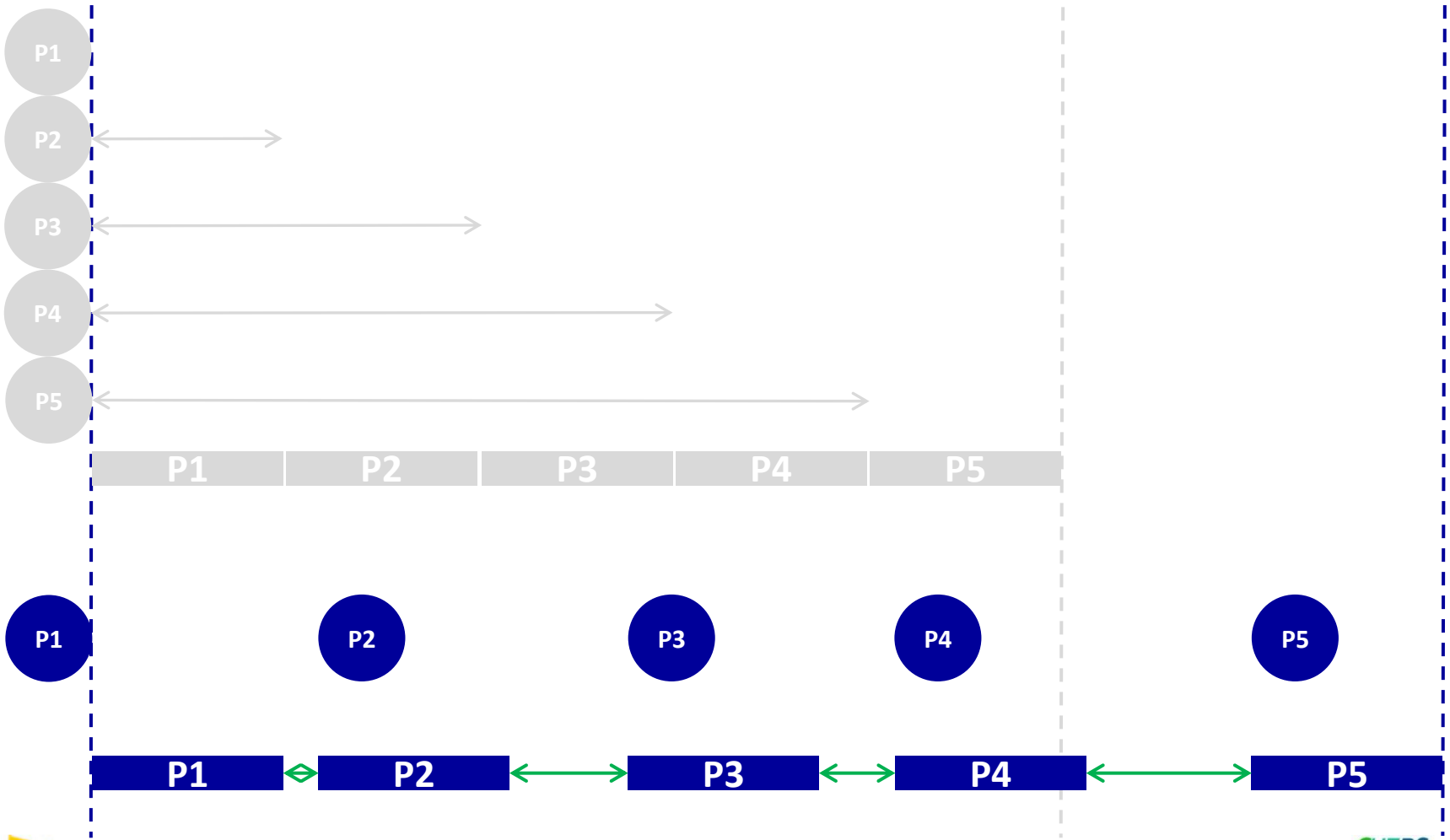
- Stochastic MIP model
  - Large number of constraints
  - Using big M in constraints results in weak relaxations
  - Numerical experiments suggest that LPT sequencing rule is optimal
- Stochastic LP model
  - Assuming LPT and FIFO rules, the MIP model becomes an LP which is tractable for a large number of scenarios
  - LP optimal solution within 0.1% of MIP optimal solution



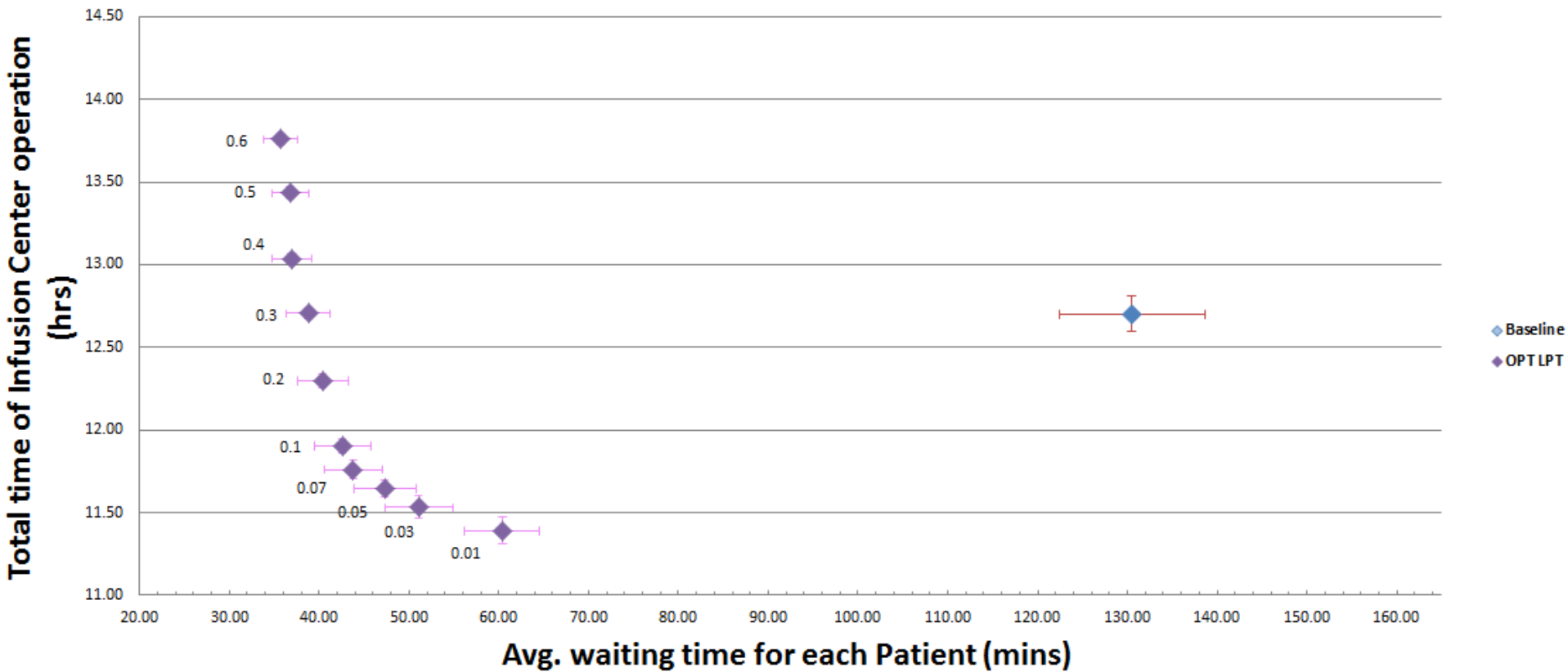
# Trade-off Concept



# Trade-off Concept

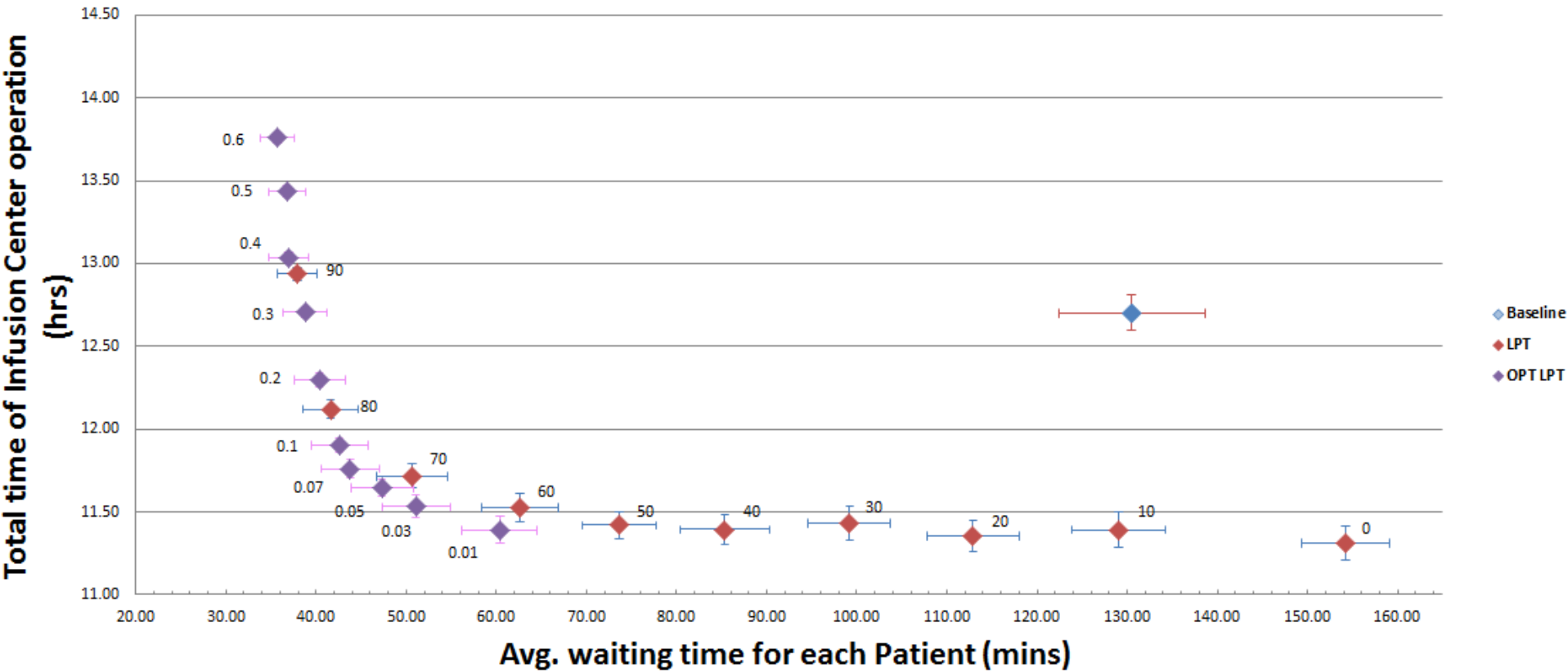


# Results

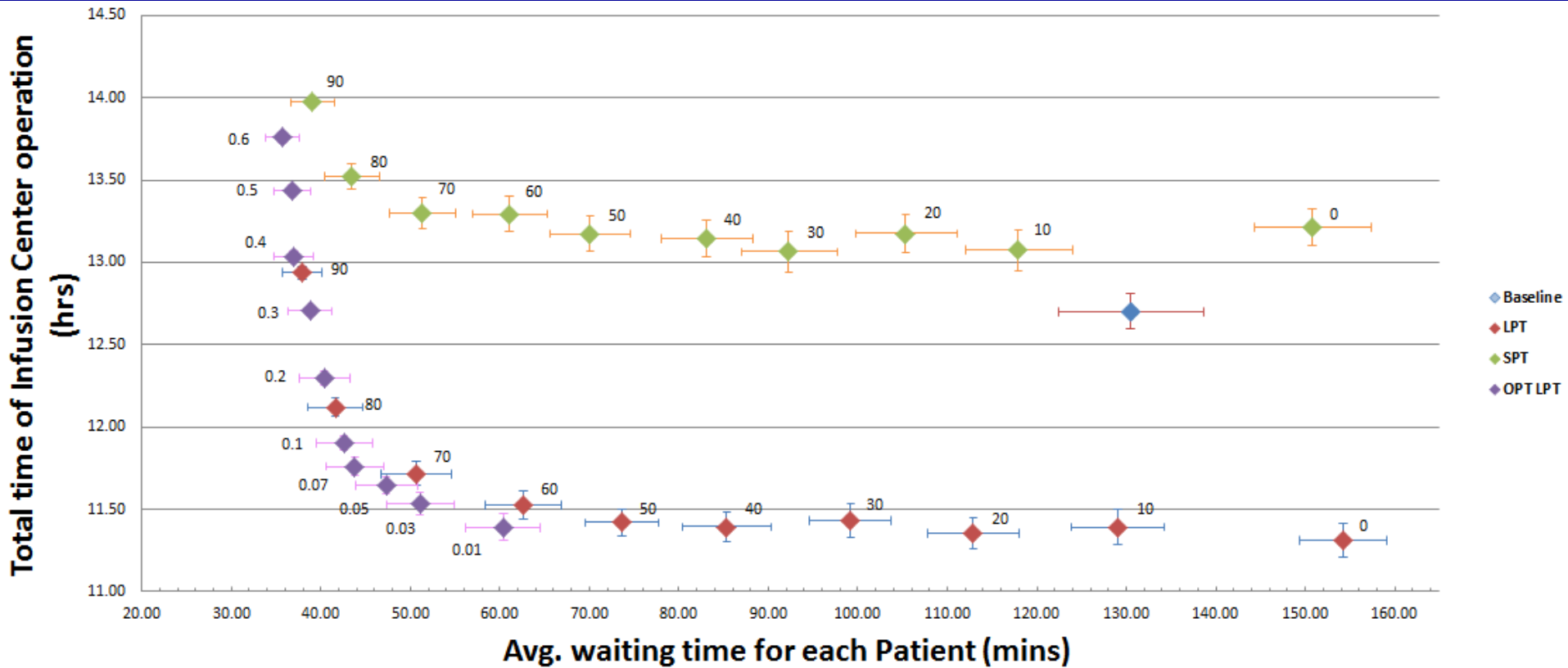




# Results



# Results



# Conclusions

- A simplified version of an infusion center scheduling process can be formulated as a stochastic integer program
- The LPT sequence appears to be optimal after solving the stochastic integer programming model
- Fixing the LPT rule for sequencing patient arrival results in an easy to solve continuous stochastic program
  - Performs slightly better than LPT heuristic



# Future Steps

- Development of a heuristic that can be easily implemented by schedulers
- Improve stochastic models
- Enhancing simulation model
  - Addition of oncology clinic
  - 2-day model evaluation
- 2-day model survey



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