

Scheduling Healthcare Providers Using Optimization

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Problem Statement

The University of Michigan Medical School (UMMS) offers comprehensive training programs across many disciplines



Coordinating the long- and short-term schedules for all these trainees is a complex challenge

Traditional Approach:

Hand-made schedules built by the Chief Resident or some other administrator

Benefits

- 1) Intimate knowledge of problem
- 2) Administrative consolidation
- 3) Streamlined approval process

Drawbacks

- 1) Time-consuming construction
- 2) High cognitive demand
- 3) Limited tradeoff consideration

Importance of Schedule Quality:

Schedule quality impacts

- Patient access, care quality, safety, and satisfaction
- Training quality and burnout rates
- Clinical/administrative workflow

The Problem:

The construction process is resource-intensive yet often fails to satisfy the individual & collective needs of stakeholders for long- and short-term schedules

Objective:

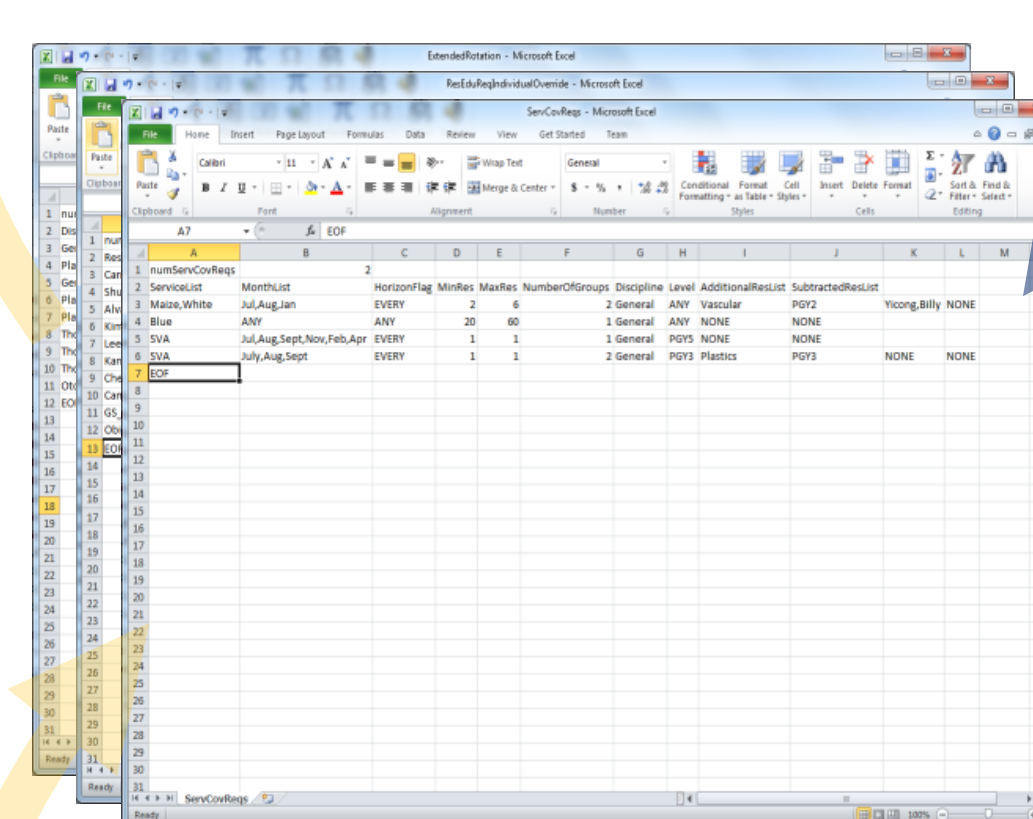
Develop decision support systems (DSS) to enable fast construction of high-quality rotation & monthly schedules while improving measures of quality.

Annual Blocks: Solution Approach

Sets
R: residents
C: resident categories
S: services
M: months
Parameters
 $\alpha_{rc} \in \{0,1\}$: whether resident r fits category c
 L_{rcm}, U_{rcm} : lower, upper bounds on staffing of residents fitting category c in service s during month m
 L_{rsm}, U_{rsm} : lower, upper bounds on months resident r must spend on service s
Decision Variables
 $x_{rcsm} \in \{0,1\}$: whether resident r is assigned to service s in month m
 $\forall r \in R, s \in S, m \in M$
Objective Function
 $\min 0$
Constraints
 $\sum_{r \in R} x_{rcsm} = 1, \forall r \in R, m \in M$
 $\sum_{s \in S} x_{rcsm} \leq \mu_{rcs}, \forall r \in R, s \in S$
 $L_{rcm} \leq \sum_{s \in S} x_{rcsm} \leq U_{rcm}, \forall r \in R, c \in S, m \in M$
 $L_{rsm} \leq \sum_{m \in M} x_{rcsm} \leq U_{rsm}, \forall r \in R, s \in S$

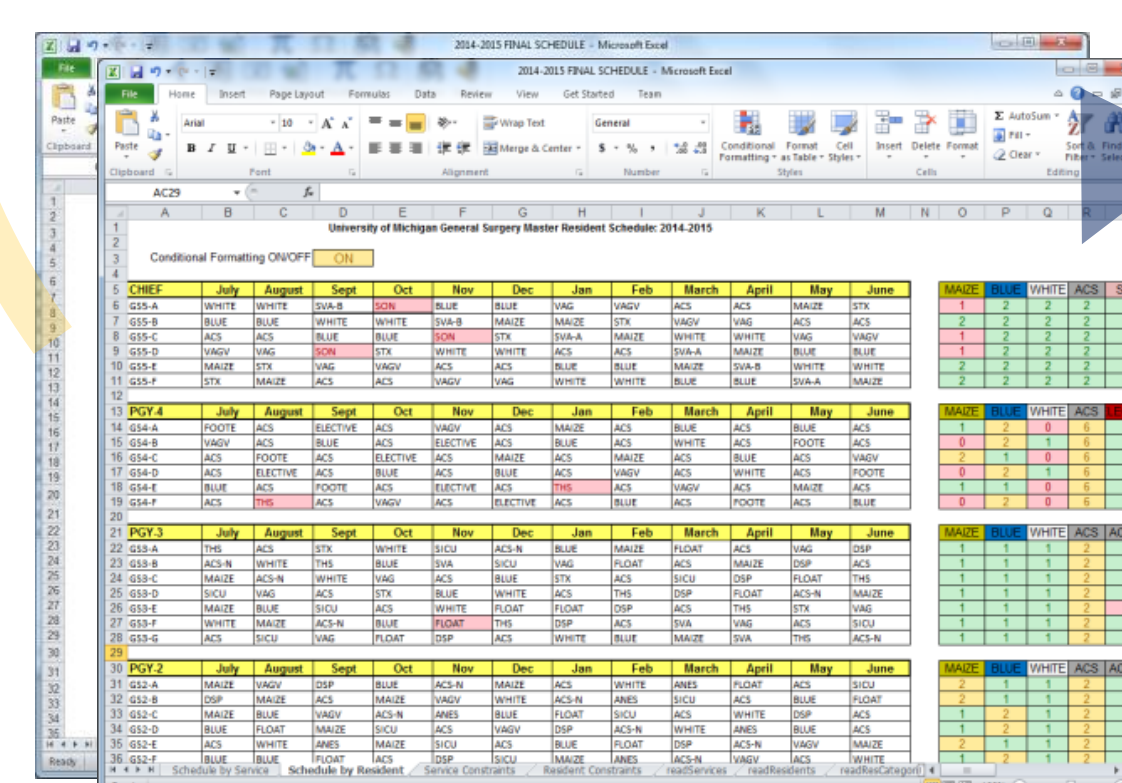
2. Encode

Written in C++ using CPLEX 12.4, implemented in Visual Studio 2012



4. Solve

Software solves to optimality under input conditions

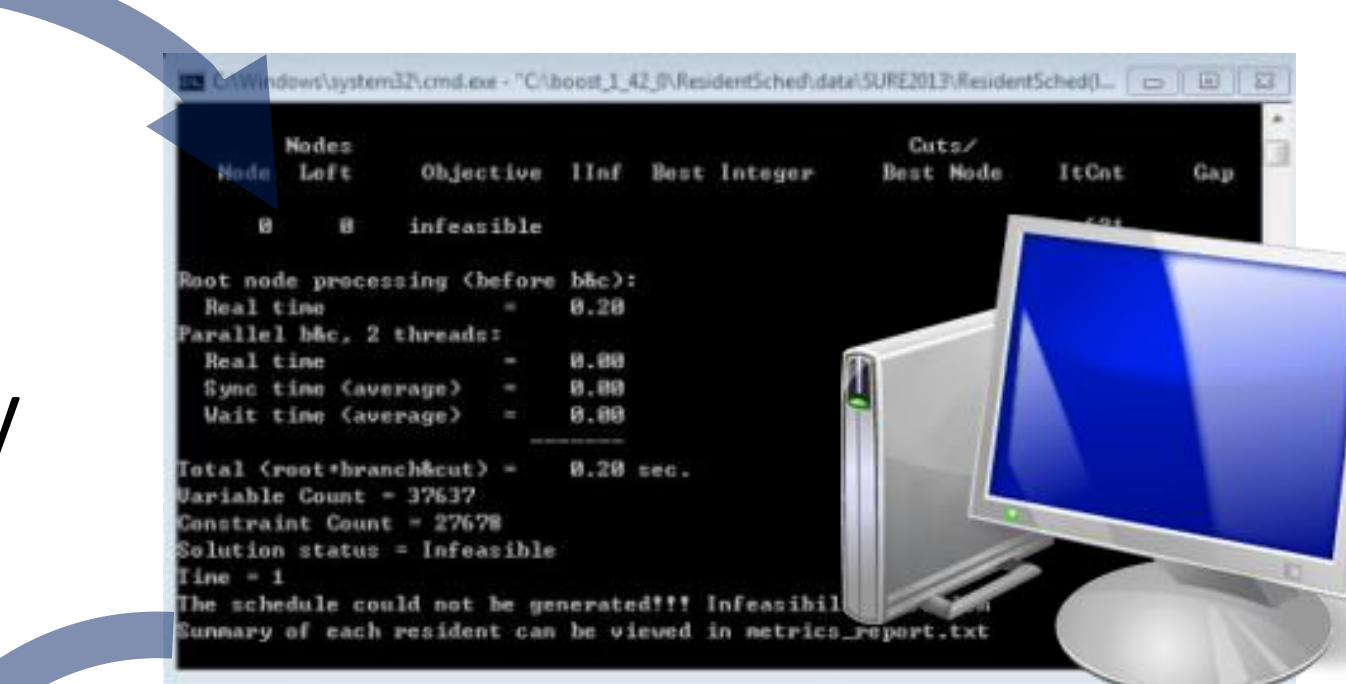


1. Formulate

Two models, each customized to specific needs of the program(s)

3. Load

Inputs provided in a collection of .txt, .csv, and .xls files



5. Review

Schedule and metric reports generated for presentation to administrators

Monthly Schedules: Solution Approach

Metrics:

- Total Shift Equity (TSE)
- Bad-Sleep Patterns (BSP)
- Night Shift Equity (NSE)
- Post-Continuity Clinic Shifts (PCC)

Preferences? Weights? Trade-off?

Feasibility Optimization Problem:

- ✗ Quantifying objective weights (w_i) is difficult due to
 - Non-linearity
 - Subjectivity
- ✓ Feasibility with metric bounds offers
 - Flexibility
 - Speed

$$\begin{aligned} \text{Min } & w_1(TSE) + w_2(NSE) + w_3(BSP) + w_4(PCC) \\ \text{s. t. } & \text{"rules/requirements"} \\ & x_{rsm} \in \{0,1\} \\ & lb_{TSE} \leq (TSE) \leq ub_{TSE} \\ & lb_{NSE} \leq (NSE) \leq ub_{NSE} \\ & lb_{BSP} \leq (BSP) \leq ub_{BSP} \\ & lb_{PCC} \leq (PCC) \leq ub_{PCC} \end{aligned}$$

Iterative Improvement:

Engage Chief Resident to review, revise and finalize the schedule

Resident Name	Number of Shifts	Number of Night Shifts	Number of Post-CC Shifts	Number of Bad Sleep Patterns
Stumpus	8 (7,9)	2 (2,3)	0 (0,1)	0 (0,0)
Schwein	8 (7,10)	2 (2,3)	0 (0,1)	0 (0,0)
Grum	8 (7,9)	2 (2,3)	1 (0,1)	0 (0,0)

Monthly Schedules: Impact/Results

Implementation Results:

- Statistically significant improvement in 3 of 4 metrics
- Reduced schedule creation time

20 hrs / month → 1 hr / month

Next Steps:

- Generalize models into universal formulation
- Extend models to address other residency programs' needs
- Apply algorithm to apply maximally feasible sets of requests

Acknowledgements

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Annual Block: Impact/Results

The **Surgical Block Scheduling** DSS aided schedule construction for:

118 residents
10 programs
62 services

Solve time per iteration:

< 5 min

217/1199 of UMMS residents scheduled

The **Pediatrics Block Scheduling** DSS aided schedule construction for:

99 residents
2 programs
14 services

Solve time per iteration:

< 3 min

98% of resident requests satisfied

	PGY1	PGY2	PGY3
Jul	GEN / GEN	ADOLESC	ELECTIVE / V7
Aug	NICU	PER / ELECTIVE	GEN / GEN
Sep	PEDS SURG	ELECTIVE / V7	PER / NITES
Oct	BEHAVIOR	DAY SR / PHO	PICU
Nov	V14 / NITES	PER / ELECTIVE	ELECTIVE / ELECTIVE
Dec	NEWBORN / PHO	ELECTIVE / V7	ELECTIVE / V7
Jan	GEN / GEN	SILVER / SILVER	NICU
Feb	PER / PER	V14 / NITES	ELECTIVE / V7
Mar	NITES / NEWBORN	ELECTIVE / ELECTIVE	ELECTIVE / V7
Apr	PHO / V10	PCH	GEN / GEN
May	GEN / GEN	PICU	NITES / PER
Jun	GEN / GEN	NICU	PCH

Sample rotation for Pediatrics
24 residents per level per year

Quality ↑

Time ↓