

Determining an Optimal Schedule for Pre-Mixing Chemotherapy Drugs

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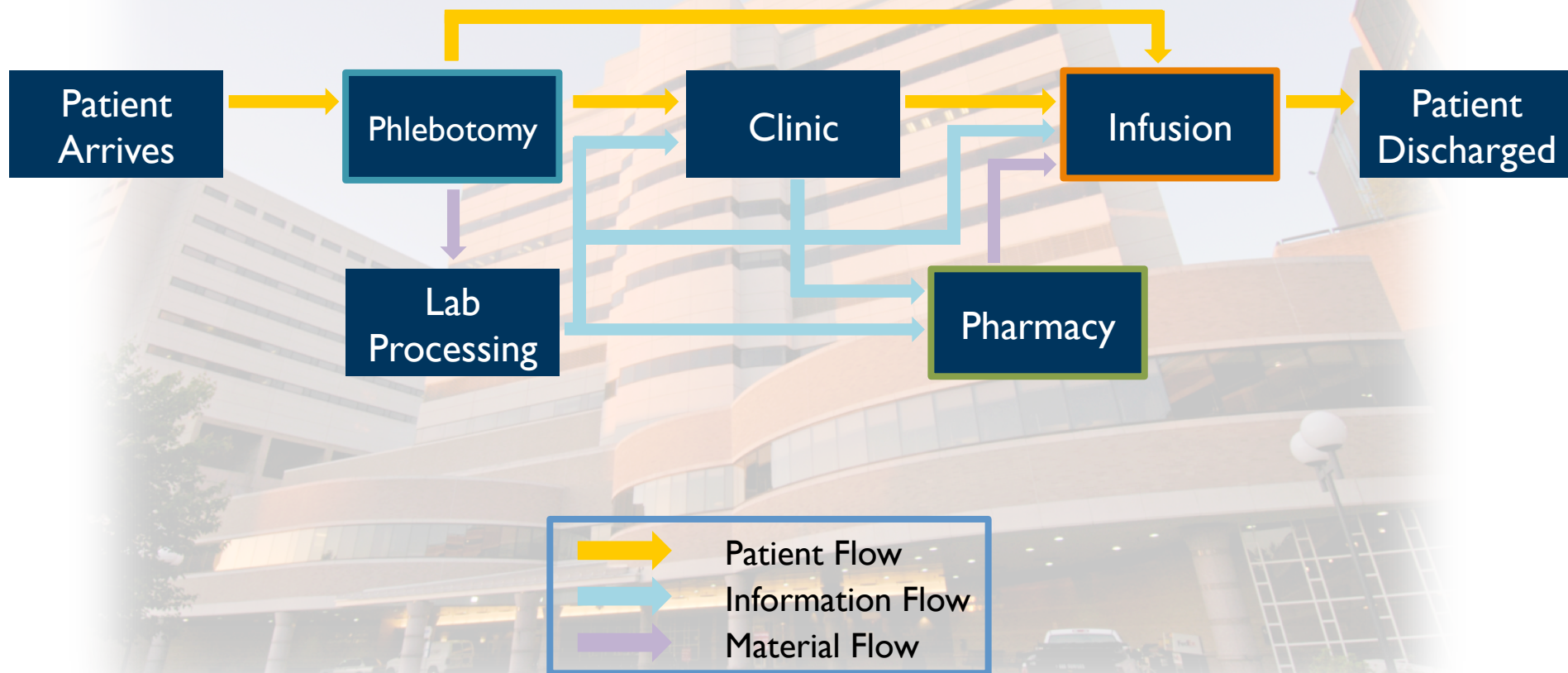
- Background
 - General Patient Flow
 - Define Pre-mix
 - Goal
 - Motivation
 - Literature
- Problem Description
 - Probabilities of wasting drugs
 - Static Model
- Future Steps



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Infusion Overview



What is Pre-mix ?

- Anytime you mix a drug before a patient is deemed ready to receive it
 - Generally you don't pre-mix drugs due to risk in wastage cost
 - Consider the trade off between waste cost and reduced patient waiting time



- Will only mix drugs during a fixed window of time before patients arrive
 - 6am-8am
- Have a fixed list of drugs they are willing to mix
 - Based on cost and common use



- Reduce patient waiting times
- Best case without pre-mix
 - Patient will wait duration of mixing drug (~30-60 min)



"This is the pre-pre-pre-waiting room, sir. You have 3 other waiting rooms to wait in before you see the doctor...if it isn't too late in the day."

- Cancer
 - Second leading cause of death in the U.S.
 - ~1.6 million estimated cases in 2015
 - More than half require chemotherapy treatment
- Infusion centers
 - Increased outpatient demand leads to undesirable outcomes such as:
 - Increased patient waiting times
 - Overworked staff

- Pre-mixing does prove to have positive outcomes
 - Masselink, I., Mijden, T., Litvak, N., & Vanberkel, P. (2011). *Preparation of chemotherapy drugs: Planning policy for reduced waiting times.*
- Cost associated with patient wait in cancer care
 - Yabroff, K. Robin, et al. "Patient time costs associated with cancer care." *Journal of the National Cancer Institute* 99.1 (2007): 14-23.
- Deciding when to mix Chemo drugs
 - Mazier, Alexandre, Jean-Charles Billaut, and Jean-François Tournamille. "Scheduling preparation of doses for a chemotherapy service." *Annals of Operations Research* 178.1 (2010): 145-154.

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- Hang-by time: the time duration that a drug has until it must be administered to patient.
- Deferral: Patient is too ill to receive treatment
- No show: Patient missed appointment without calling in

Description of Problem (Static)

- We will also consider having a fixed window for pre-mix
- Assumptions
 - All drugs will last for all patients scheduled that day (most last 12 hours)
 - Only make L drugs at a time
 - All drugs take 30 minutes to make

Probability of Wasting a Drug

- We first say all patients have a probability of p to defer/no show on any given day. Assume we have m_d patients scheduled to receive the same drug d on a given day. We want the probability of wasting each dose we decide to premix.

Probability of Wasting a Drug

- We first say all patients have a probability of p to defer/no show on any given day. Assume we have m_d patients scheduled to receive the same drug d on a given day. We want the probability of wasting each dose we decide to premix.
- Let $m_d=4$

$$Prob(\text{Wasting } 1^{st} \text{ dose}) = p^4$$

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$$Prob(\text{Wasting } 2^{nd} \text{ dose}) = \binom{4}{3} p^3 (1 - p) + p^4$$

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General

$$Prob(\text{Wasting } n^{th} \text{ dose}) = \sum_{i=1}^n \binom{m_d}{m_d - i + 1} p^{m_d - i + 1} (1 - p)^{i-1}$$

- The previous formulation considers all patients to have equal probability of deferral. However this could depend on
 - age
 - sex
 - treatment
 - type of cancer
 - etc.



Probability of Wasting a Drug (Cont.)

- Let's now consider the probability of wasting a particular dose given patient i has a probability of deferral/no show p_i
- Let's define a new set S_d which is the total number of patients scheduled to receive drug d for the day. $S_d = \{1, 2, \dots, m_d\}$

Probability of Wasting a Drug (Cont.)

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$$Prob(\text{Wasting } 2^{nd} \text{ dose}) = \sum_{i \in S_d} \left[(1 - p_i) \prod_{j \in S_d \setminus i} (p_j) \right] + \prod_{i \in S_d} p_i$$

Probability of Wasting a Drug (Cont.)

- Let's now consider the probability of wasting a particular dose given patient i has a probability of deferral/no show p_i .
- Let's define a new set S_d which is the total number of patients scheduled to receive drug d for the day. $S_d = \{1, 2, \dots, m_d\}$.

$$Prob(\text{Wasting } 1^{st} \text{ dose}) = \prod_{i \in S_d} p_i$$

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$$Prob(\text{Wasting } 3^{rd} \text{ dose}) = \sum_{i \in S_d} \sum_{j \in S_d \setminus i} \left[(1 - p_i)(1 - p_j) \prod_{k \in S_d \setminus \{i, j\}} p_k \right] + \sum_{i \in S_d} \left[(1 - p_i) \prod_{j \in S_d \setminus i} (p_j) \right] + \prod_{i \in S_d} p_i$$

Probability of Wasting a Drug (Cont.)

- Currently receiving/analyzing data to determine how to best categorize patients
- Current model will only vary the probability of deferral by drug, not by patient type



Sets

- D: set of drugs d (e.g. 50 mg of Taxotere)
- T: set of time units (each being 30 min)

Variables

$$x_{nt}^d = \begin{cases} 1 & \text{if we mix the } n\text{th dose of drug } d \text{ at time } t \\ 0 & \text{o.w.} \end{cases}$$

$$y_n^d = \begin{cases} 1 & \text{if we don't mix the } n\text{th dose of drug } d \\ 0 & \text{o.w.} \end{cases}$$

- We first define our Expected Waste cost of a drug with the following:

$$E_n^d[\text{waste cost}] = \sum_{w=1}^n c_d P_d(w)$$

- Then we maximize the difference between Projected Savings and Expected Waste

$$\text{maximize } \sum_d \sum_n \sum_t (\Delta_d - E_n^d[\text{waste cost}]) * x_{nt}^d$$

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
- M : very large number

$$\sum_t x_{nt}^d + y_n^d = 1 \quad \forall d, n \quad (1)$$

Relate our auxiliary variable to the decision variable

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
- M : very large number

$$\sum_t x_{nt}^d + y_n^d = 1 \quad \forall d, n \quad (1)$$

$$y_n^d \leq y_{n+1}^d \quad \forall d, n = 1..n[d] - 1 \quad (2)$$

Must make the first dose before making 2nd, 3rd, ...

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
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$$\sum_t x_{nt}^d + y_n^d = 1 \quad \forall d, n \quad (1)$$

$$y_n^d \leq y_{n+1}^d \quad \forall d, n = 1..n[d] - 1 \quad (2)$$

$$\sum_t tx_{nt}^d \leq \sum_t tx_{n+1t}^d + M * y_{n+1}^d \quad \forall n, d \quad (3)$$

Dose ordering

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
- M : very large number

$$\sum_t x_{nt}^d + y_n^d = 1 \quad \forall d, n \quad (1)$$

$$y_n^d \leq y_{n+1}^d \quad \forall d, n = 1..n[d] - 1 \quad (2)$$

$$\sum_t tx_{nt}^d \leq \sum_t tx_{n+1t}^d + M * y_{n+1} \quad \forall n, d \quad (3)$$

$$\sum_d \sum_n x_{nt}^d \leq L \quad \forall t \quad (4)$$

Only make L at a time

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
- M : very large number

$$\sum_t x_{nt}^d + y_n^d = 1 \quad \forall d, n \quad (1)$$

$$y_n^d \leq y_{n+1}^d \quad \forall d, n = 1..n[d] - 1 \quad (2)$$

$$\sum_t tx_{nt}^d \leq \sum_t tx_{n+1t}^d + M * y_{n+1}^d \quad \forall n, d \quad (3)$$

$$\sum_d \sum_n x_{nt}^d \leq L \quad \forall t \quad (4)$$

$$\sum_t x_{nt}^d \leq 1 \quad \forall n, d \quad (5)$$

Can only make the n th dose of a drug once

Parameters

- Δ_d : the reward/savings for mixing drug d
- T : the total time units for the premix period
- c_d : the cost of drug d
- $n[d]$: the number of doses needed for each drug based on the scheduled patients
- M : very large number

Example

- Suppose we have patients scheduled to receive 15 different drugs.
- Each takes 30 min to make

| Drug | Hang by | Price | Currently pre-mixed | Treatment for |
|------------------|---------|---------|---------------------|---|
| Carboplatin | 12 hrs | 2.52 | Yes | Cancer of the ovaries, head, and neck |
| Paclitaxel | 12 hrs | 4.10 | Yes | Cancer in the lungs, ovary, or breast |
| Cyclophosphamide | 12 hrs | 879.00 | Yes | Leukemia and lymphomas, and nephrotic syndrome |
| Folotyn | 12 hrs | 4637.21 | No | T-cell lymphoma |
| Adcetris | 12 hrs | 6516.00 | No | Treats Hodgkin's lymphoma and systemic anaplastic large cell lymphoma |

Example Scenarios

Scenario 1

| | |
|------------|-----------------------|
| Reward | 1 for all drugs |
| # of Doses | 2 for each drug |
| $P_d(n)$ | $p=.25$ for all drugs |

Example Scenarios

| | Scenario 1 | Scenario 2 |
|------------|-----------------------|-----------------------|
| Reward | 1 for all drugs | 11.67 for all drugs |
| # of Doses | 2 for each drug | 2 for each drug |
| $P_d(n)$ | $p=.25$ for all drugs | $p=.25$ for all drugs |

Example Scenarios

| | Scenario 1 | Scenario 2 | Scenario 3 |
|------------|-----------------------|-----------------------|---|
| Reward | 1 for all drugs | 11.67 for all drugs | 11.67 for all drugs |
| # of Doses | 2 for each drug | 2 for each drug | 2 for each drug |
| $P_d(n)$ | $p=.25$ for all drugs | $p=.25$ for all drugs | inverse to cost of drug ranging from .02 to .30 |

Example Scenarios

| | Scenario 1 | Scenario 2 | Scenario 3 | Scenario 4 |
|------------|-----------------------|-----------------------|---|-----------------------------------|
| Reward | 1 for all drugs | 11.67 for all drugs | 11.67 for all drugs | 11.67 for all drugs |
| # of Doses | 2 for each drug | 2 for each drug | 2 for each drug | 1-2 lower cost 3-5 higher cost |
| $P_d(n)$ | $p=.25$ for all drugs | $p=.25$ for all drugs | inverse to cost of drug ranging from .02 to .30 | $p=.25$ for all drugs |

Example Scenarios

| | Scenario 1 | Scenario 2 | Scenario 3 | Scenario 4 | Scenario 5 |
|------------|-----------------------|-----------------------|---|-----------------------------------|---|
| Reward | 1 for all drugs | 11.67 for all drugs | 11.67 for all drugs | 11.67 for all drugs | 11.67 for all drugs |
| # of Doses | 2 for each drug | 2 for each drug | 2 for each drug | 1-2 lower cost 3-5 higher cost | 1-2 lower cost 3-5 higher cost |
| $P_d(n)$ | $p=.25$ for all drugs | $p=.25$ for all drugs | inverse to cost of drug ranging from .02 to .30 | $p=.25$ for all drugs | inverse to cost of drug ranging from .02 to .30 |

Results

| Drugs | Cost |
|-------|------------|
| A | \$1.61 |
| B | \$2.52 |
| C | \$4.10 |
| D | \$6.80 |
| E | \$16.56 |
| F | \$83.40 |
| G | \$91.54 |
| H | \$155.56 |
| I | \$367.02 |
| J | \$698.60 |
| K | \$879.00 |
| L | \$1,158.84 |
| M | \$2,389.39 |
| N | \$4,637.21 |
| O | \$6,516.00 |
| TOTAL | — |

Results

| Drugs | Cost | Scen. 1 |
|-------|------------|---------|
| A | \$1.61 | 2 |
| B | \$2.52 | 1 |
| C | \$4.10 | 1 |
| D | \$6.80 | 1 |
| E | \$16.56 | — |
| F | \$83.40 | — |
| G | \$91.54 | — |
| H | \$155.56 | — |
| I | \$367.02 | — |
| J | \$698.60 | — |
| K | \$879.00 | — |
| L | \$1,158.84 | — |
| M | \$2,389.39 | — |
| N | \$4,637.21 | — |
| O | \$6,516.00 | — |
| TOTAL | — | 5 |

Results

| Drugs | Cost | Scen. 1 | Scen. 2 |
|-------|------------|---------|---------|
| A | \$1.61 | 2 | 2 |
| B | \$2.52 | 1 | 2 |
| C | \$4.10 | 1 | 2 |
| D | \$6.80 | 1 | 1 |
| E | \$16.56 | — | 1 |
| F | \$83.40 | — | — |
| G | \$91.54 | — | — |
| H | \$155.56 | — | — |
| I | \$367.02 | — | — |
| J | \$698.60 | — | — |
| K | \$879.00 | — | — |
| L | \$1,158.84 | — | — |
| M | \$2,389.39 | — | — |
| N | \$4,637.21 | — | — |
| O | \$6,516.00 | — | — |
| TOTAL | — | 5 | 8 |

Results

| Drugs | Cost | Scen. 1 | Scen. 2 | Scen. 3 |
|-------|------------|---------|---------|---------|
| A | \$1.61 | 2 | 2 | 2 |
| B | \$2.52 | 1 | 2 | 2 |
| C | \$4.10 | 1 | 2 | 2 |
| D | \$6.80 | 1 | 1 | 1 |
| E | \$16.56 | — | 1 | 1 |
| F | \$83.40 | — | — | — |
| G | \$91.54 | — | — | — |
| H | \$155.56 | — | — | — |
| I | \$367.02 | — | — | — |
| J | \$698.60 | — | — | — |
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| L | \$1,158.84 | — | — | — |
| M | \$2,389.39 | — | — | — |
| N | \$4,637.21 | — | — | — |
| O | \$6,516.00 | — | — | — |
| TOTAL | — | 5 | 8 | 8 |

Results

| Drugs | Cost | Scen. 1 | Scen. 2 | Scen. 3 | Scen. 4 |
|-------|------------|---------|---------|---------|---------|
| A | \$1.61 | 2 | 2 | 2 | 2 |
| B | \$2.52 | 1 | 2 | 2 | 2 |
| C | \$4.10 | 1 | 2 | 2 | 1 |
| D | \$6.80 | 1 | 1 | 1 | 1 |
| E | \$16.56 | — | 1 | 1 | 1 |
| F | \$83.40 | — | — | — | — |
| G | \$91.54 | — | — | — | — |
| H | \$155.56 | — | — | — | — |
| I | \$367.02 | — | — | — | — |
| J | \$698.60 | — | — | — | — |
| K | \$879.00 | — | — | — | 1 |
| L | \$1,158.84 | — | — | — | — |
| M | \$2,389.39 | — | — | — | — |
| N | \$4,637.21 | — | — | — | — |
| O | \$6,516.00 | — | — | — | — |
| TOTAL | — | 5 | 8 | 8 | 8 |

Results

| Drugs | Cost | Scen. 1 | Scen. 2 | Scen. 3 | Scen. 4 | Scen. 5 |
|-------|------------|---------|---------|---------|---------|---------|
| A | \$1.61 | 2 | 2 | 2 | 2 | — |
| B | \$2.52 | 1 | 2 | 2 | 2 | 1 |
| C | \$4.10 | 1 | 2 | 2 | 1 | — |
| D | \$6.80 | 1 | 1 | 1 | 1 | 1 |
| E | \$16.56 | — | 1 | 1 | 1 | — |
| F | \$83.40 | — | — | — | — | — |
| G | \$91.54 | — | — | — | — | — |
| H | \$155.56 | — | — | — | — | — |
| I | \$367.02 | — | — | — | — | — |
| J | \$698.60 | — | — | — | — | 1 |
| K | \$879.00 | — | — | — | 1 | 2 |
| L | \$1,158.84 | — | — | — | — | 1 |
| M | \$2,389.39 | — | — | — | — | — |
| N | \$4,637.21 | — | — | — | — | — |
| O | \$6,516.00 | — | — | — | — | 2 |
| TOTAL | — | 5 | 8 | 8 | 8 | 8 |

Results

| Drugs | Cost | Scen. 1 | Scen. 2 | Scen. 3 | Scen. 4 | Scen. 5 |
|-------|------------|---------|---------|---------|---------|---------|
| A | \$1.61 | 2 | 2 | 2 | 2 | — |
| B | \$2.52 | 1 | 2 | 2 | 2 | 1 |
| C | \$4.10 | 1 | 2 | 2 | 1 | — |
| D | \$6.80 | 1 | 1 | 1 | 1 | 1 |
| E | \$16.56 | — | 1 | 1 | 1 | — |
| F | \$83.40 | — | — | — | — | — |
| G | \$91.54 | — | — | — | — | — |
| H | \$155.56 | — | — | — | — | — |
| I | \$367.02 | — | — | — | — | — |
| J | \$698.60 | — | — | — | — | 1 |
| K | \$879.00 | — | — | — | 1 | 2 |
| L | \$1,158.84 | — | — | — | — | 1 |
| M | \$2,389.39 | — | — | — | — | — |
| N | \$4,637.21 | — | — | — | — | — |
| O | \$6,516.00 | — | — | — | — | 2 |
| TOTAL | — | 5 | 8 | 8 | 8 | 8 |

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- Static Model
 - Consider
 - Hang-by time for various drugs
 - Preparation time for various drugs
 - Continue working with data collection to run logistical regression
 - How to categorize various types of patients
- Dynamic Model
 - Goal: To find an optimal drug-mixing schedule throughout the day and update as we observe patient deferrals

Thank You!

Contacts

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CHEPS

<http://cheps.engin.umich.edu>



- States – 3-dimensional
 - t : Time of day we are making the decision
 - O : List of orders for patients scheduled that day
 - S : Inventory of premixed drugs
- Actions
 - Mix a certain drug or not mix at $A = \{o \in O, \emptyset\}$
- Stages
 - $[0, T]$ in 15 min intervals
- Rewards
 - Expected reward of mixing drug o at time t

Replace with updated version

$$v(t, O, S) = \max_{o \in O} \{R(o, t) + p(o)v(t', O \setminus o, S \cup \{o\}) + (1 - p(o))v(t', O \setminus o, S)\}$$

where:

$p(o)$ is the probability of deferral of patient receiving order o

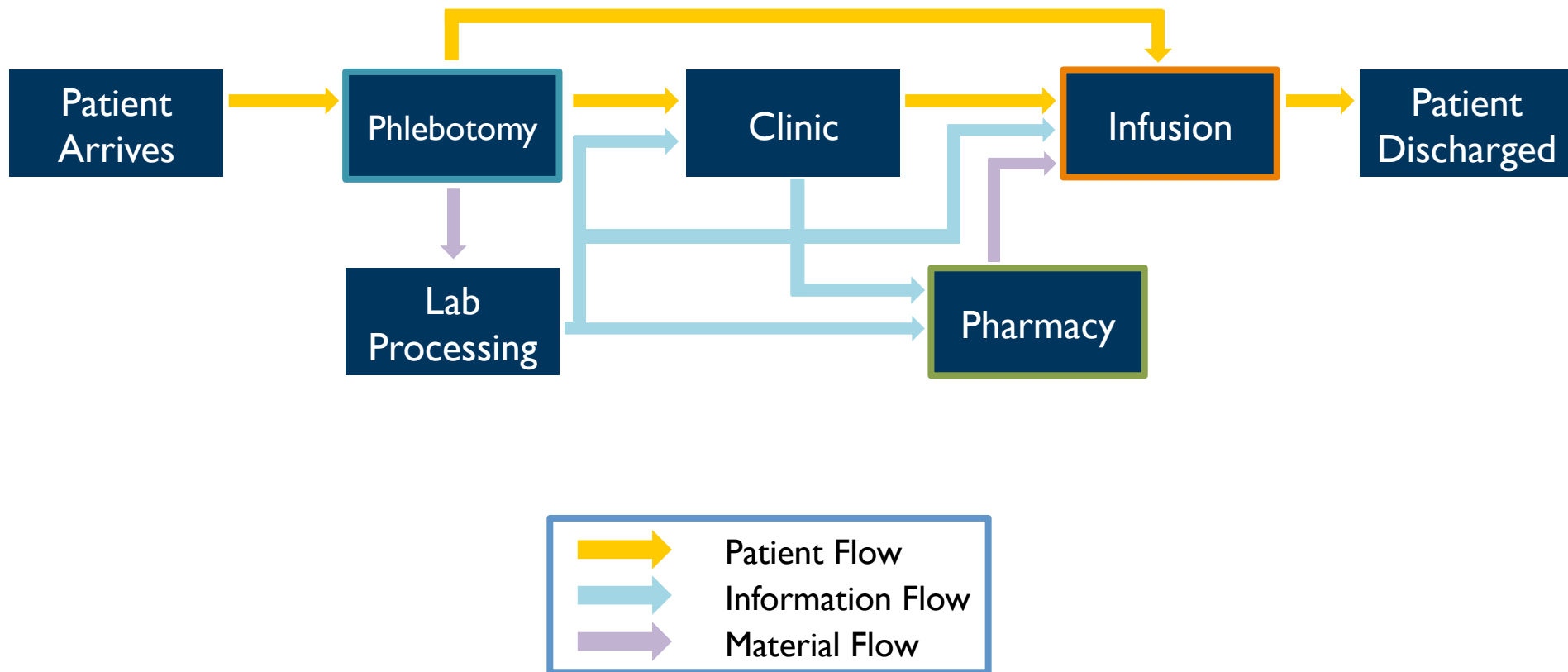
$R(o, t)$ is the expected reward of preparing order o at time t

$v(t', O', S')$ is the expected reward after we prepared order o .

Work started by Sarah Bach Jeremy Casting

- For $|O|$ moderately low
 - Use backward induction
- For $|O|$ otherwise
 - State space blows up!
 - Approximate Dynamic programming

Infusion Overview



Scenario 1

Objective Value = 3.36

$E[\text{Waste}] = 1.64$

Scenario 3

Objective Value = 87.82

$E[\text{Waste}] = 5.575$

Scenario 3

Objective Value = 87.7

$E[\text{Waste}] = 5.70$

Scenario 4

Objective Value = 88.74

$E[\text{Waste}] = 4.66025$

Scenario 5

Objective Value = 92.23

$E[\text{Waste}] = 1.17$